

# BILATERAL TRADE MODELING WITH GRAPH NEURAL NETWORKS

**Kobby Panford-Quainoo**

African Institute for Mathematical Sciences,  
Kigali, Rwanda

[kpanford-quainoo@aimsammi.org](mailto:kpanford-quainoo@aimsammi.org)



@panfordkobby

**Avishek Joey Bose**

McGill University, MILA  
Montreal, Canada

[joey.bose@mail.mcgill.ca](mailto:joey.bose@mail.mcgill.ca)

@bose\_joey

**Michaël Defferrard**

École Polytechnique Fédérale de Lausanne  
Lausanne, Switzerland

[michael.defferrard@epfl.ch](mailto:michael.defferrard@epfl.ch)

@m\_deff

# Our work

- Data-driven and graph representation learning approach to modeling bilateral trade between countries
- Predicting potential trade partners → link prediction problem
- Classifying countries into income levels → node classification problem
  - Income Levels
    - High
    - Upper-middle
    - Lower-middle
    - Lower

# Motivation I

## Gravity model

$$F_{ij} = M \frac{GDP_i \cdot GDP_j}{D_{ij}}$$

Trade flow (i, j)  $\rightarrow$   $F_{ij}$

$M$  constant  $\leftarrow$

GDP of country i  $\rightarrow$   $GDP_i$

GDP of country j  $\leftarrow$   $GDP_j$

Geographical distance (i, j)  $\leftarrow$   $D_{ij}$

# Motivation I

## Gravity Model

$$F_{ij} = M \frac{GDP_i \cdot GDP_j}{D_{ij}}$$

$$\ln F_{ij} = c_0 + c_1 \ln \underline{GDP}_i + c_2 \ln \underline{GDP}_j + c_3 \ln \underline{D}_{ij} + \underline{c_4 d + c_5 P_{ij} + \epsilon_{ij}}$$

- $c_k$  - hand-engineered constants
- $P_{ij}$  - political influence term
- $\epsilon_{ij}$  - error correction term
- $d$  - cultural influence

# Motivation I

## Gravity Model

$$F_{ij} = M \frac{GDP_i \cdot GDP_j}{D_{ij}}$$

$$\ln F_{ij} = c_0 + c_1 \ln \underline{GDP}_i + c_2 \ln \underline{GDP}_j + c_3 \ln \underline{D}_{ij} + \underline{c_4 d + c_5 P_{ij} + \epsilon_{ij}}$$

- $c_k$  - hand-engineered constants      **Difficult!**

# Motivation I

## Gravity Model

$$F_{ij} = M \frac{GDP_i \cdot GDP_j}{D_{ij}}$$

$$\ln F_{ij} = c_0 + c_1 \ln \underline{GDP}_i + c_2 \ln \underline{GDP}_j + c_3 \ln \underline{D}_{ij} + \underline{c_4 d} + \underline{c_5 P_{ij}} + \epsilon_{ij}$$

Not informed by previous trade information !

# Motivation II

- Past trade information between countries may contribute to their income level prediction

# Data and Representation

**Data sources:** The United Nations Comtrade Database (UNCD), Kaggle

**UNCD:** Reporter-partner trade statistics

- imports and exports
- trade value in USD

**Kaggle:** Countries profile

- financial
- geographical
- income level



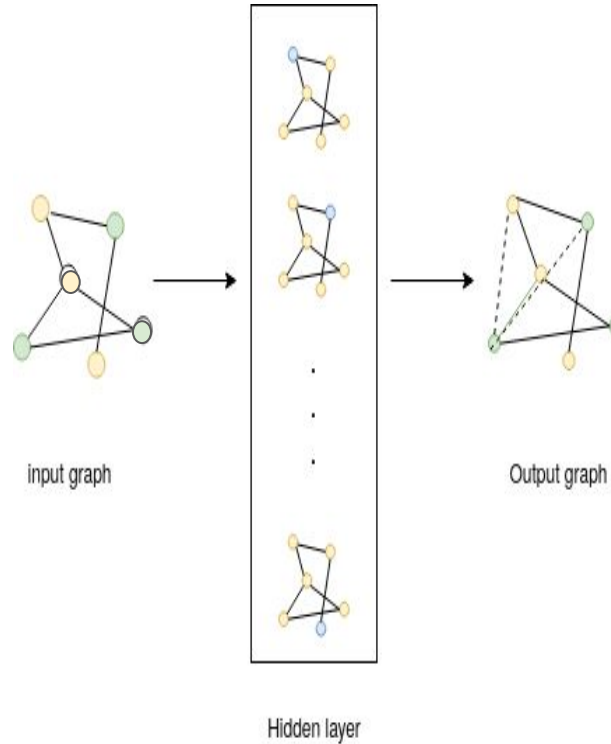
# Data and Representation

<b>Feature</b>	<b>Notation</b>	<b>Size</b>	<b>Representation</b>
nodes	$\mathcal{V}$	111	countries
Node features	$X$	38	ie. population
Edges	$A$	476	trade indicator
Edge weights	$\mathcal{E}$	476	net trade value (USD)
Node labels	$\mathcal{Y}$	4	Income levels

Table 2: summary of data features and representation

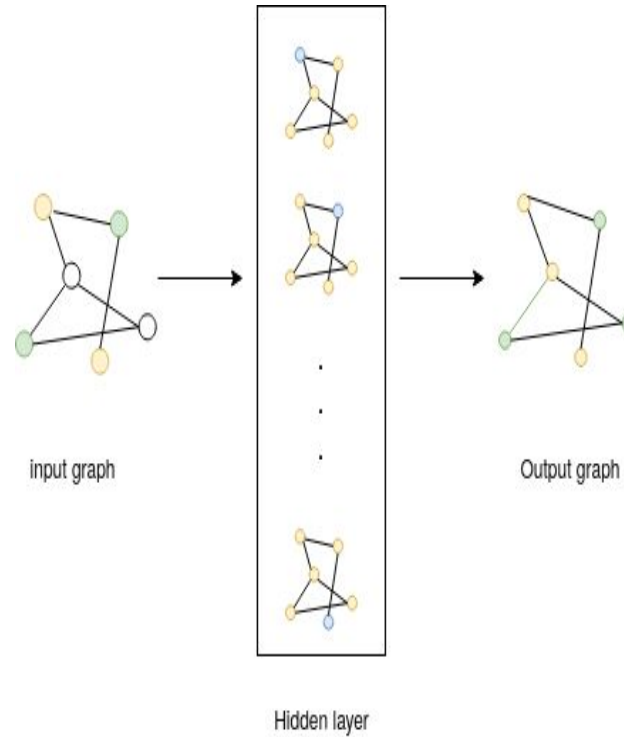
# Tasks

- Trade partner prediction:



# Tasks

- Income level prediction:



# Tasks and Exp'tal setup

- **Country Classification:** Predicting the income levels of countries
  - Graph Convolutional Network (GCN)
  - Attention-based Graph Neural Networks (AGNN)
  - Graph Attention Network (GAT)
  - Chebyshev Convolution Networks (ChebNet)
- **Trade Partner prediction:** Predicting potential trade partners in trade graph
  - Graph Autoencoder (GAE)
  - Variational Graph Autoencoder (VGAE)

# Tasks and Exp'tal setup

- Baselines -
  - Multilayer perceptron (MLP)
  - Logistic regression

# Results

	GCN	ChebNet	GAT	AGNN	Linear	Logistic Reg
Test Accuracy	<b>0.6812</b>	0.6436	0.6158	0.6003	0.6491	0.5758

Table 3: Mean node classification results, 1200 epochs, 100 runs

	GAE	VGAE
AUC	0.9840	<b>0.9888</b>
Average Precision	0.9835	<b>0.9896</b>

Table 4: Results for link prediction task

# Results - Node classification

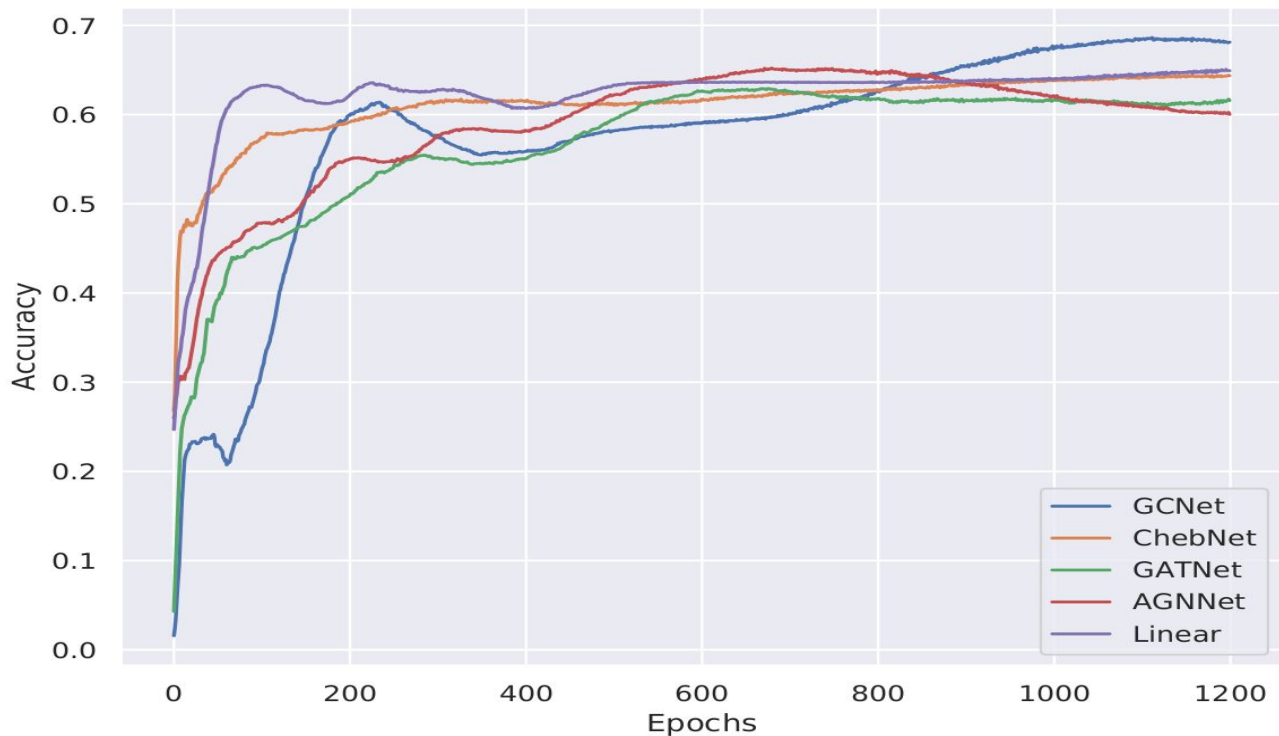


Fig 1: Model performance on node classification averaged over 100 runs

# Results - Link Prediction

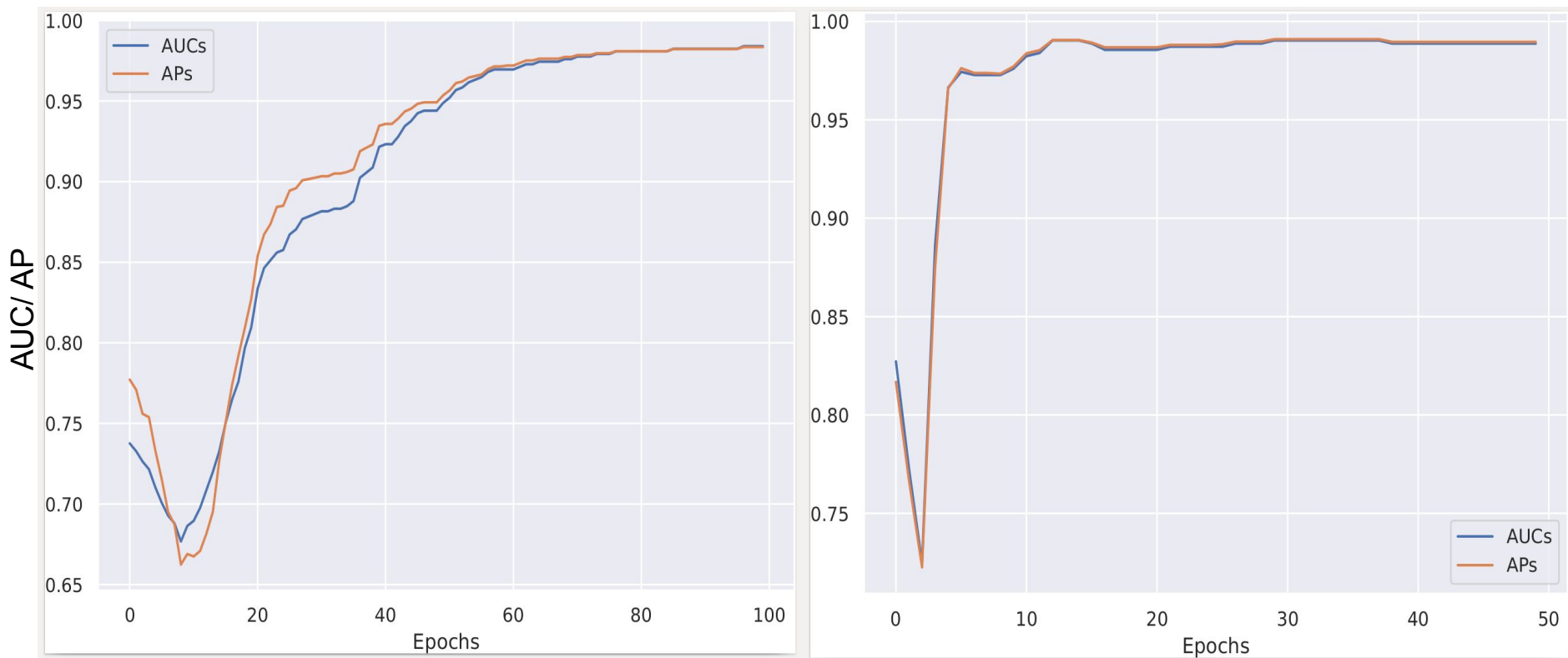


Fig 2: AUC and AP scores on reconstruction with (a) GAE (b) VGAE



# Conclusion

- Here, we encourage a graph representation learning approach to trade partner prediction and income level classification of countries.
- We use historical trade data to construct a graph for active trade relationship between countries.
- Up to 98% accuracy on predicting trading partners and 68% on income level classification
- One future direction is to consider a dynamic graph instead of a static one
  - How *trade activities* evolve with time -- temporal prediction of *edges* between countries
  - How *income levels* of countries change with time

Thank You

# References

**James E Anderson.** **The gravity model:** Annual review of economics. 2011

**Alan Deardorff.** **Determinants of bilateral trade:** Does gravity work in a neoclassical world? The Regionalization of the World Economy, pp. 7–32, 1998. doi: <https://doi:10.3386/w5377>

**Matthias Fey and Jan E. Lenssen.** **Fast graph representation learning with PyTorch Geometric.** In ICLR Workshop on Representation Learning on Graphs and Manifolds , 2019

**Elhanan Helpman, Marc Melitz, and Yona Rubinstein.** Estimating Trade Flows: Trading Partners and Trading Volumes\*. The Quarterly Journal of Economics, 123(2):441–487, 05 2008. ISSN 0033-5533. doi: 10.1162/qjec.2008.123.2.441. URL <https://doi.org/10.1162/qjec.2008.123.2.441>

**Diederik P. Kingma and Jimmy Ba.** **Adam: A method for stochastic optimization.** CoRR abs/1412.6980, 2014

**Patrick Steiner.** **Determinants of bilateral trade flows,** 2015